

## Heat Removal Factor of an Unglazed Photovoltaic Thermal Collector with a Serpentine Tube

<sup>1,2</sup>M.A.M. Rosli, <sup>1</sup>K. Sopian, <sup>1</sup>S. Mat, <sup>1</sup>M. Yusof Sulaiman and <sup>1</sup>E. Salleh

<sup>1</sup>Solar Energy Research Institute, Universiti Kebangsaan Malaysia, 43600 Bangi, Selangor, Malaysia

<sup>2</sup>Faculty of Mechanical Engineering, Universiti Teknikal Malaysia Melaka, Hang Tuah Jaya, 76100 Durian Tunggal, Melaka, Malaysia

**Abstract:** Heat removal factor ( $F_R$ ) is a vital parameter in determining the thermal efficiency of a photovoltaic thermal (PVT) system. As a main factor of thermal performance,  $F_R$  represents the ratio of the actual heat transfer to the maximum yield of heat transfer. In this study,  $F_R$  of an unglazed PVT with serpentine tube collector was determined, with focus on the flat plate thickness of the flat plate serpentine tubes. Thermal modeling was used to estimate the overall heat losses of the unglazed PVT. The highest  $F_R$  value of 0.88 was obtained in the 0.015 m-thick flat plate, followed by 0.84 in the 0.010 m-thick flat plate. The difference in  $F_R$  between the two designs was only 4.54%, which can be considered within the acceptable range for the flat plate thickness. This consideration was made based on an economical point of view and the handling issues of PVT systems.

**Key words:** Serpentine • Photovoltaic thermal (PVT) • Flat plate collector • Unglazed

### INTRODUCTION

The thermal performance of a photovoltaic thermal (PVT) collector can be determined using three important parameters, namely, the heat removal factor ( $F_R$ ), the overall losses ( $U_L$ ) and the effective transmittance absorptance  $(\tau\alpha)_{eff}$  that cover the PVT system, as follows [1]:

$$\eta_{th} = F_R(\tau\alpha)_{eff} - F_R U_L \left( \frac{T_f - T_a}{G} \right) \quad (1)$$

$F_R$  is one of the crucial parameters in determining thermal efficiency [2].  $F_R$  is defined as the ratio of useful energy to the maximum heat transfer.  $F_R$  has to be carefully determined because it is a gain factor for both  $\tau\alpha$  and  $U_L$ . Based on Equation (1),  $\tau\alpha$  should be maximum while  $U_L$  should be minimum for a PVT collector system to achieve high thermal efficiency.

$F_R$  is affected by several factors such as material selection, dimensions, geometry and operational variables. These parameters must be appropriately determined for the engineer to design a highly efficient and inexpensive collector [3, 4].

$F_R$  in various collector geometries has been investigated extensively [5]. One collector geometry type is the serpentine arrangement, the attributes of which are different from that of the conventional tube collector. Consisting of one source of water that flows from the inlet to the outlet, the serpentine arrangement is considered as a complex geometry that needs to be expressed in simple equations. It is typically made of metal materials, such as copper, stainless steel and aluminum.

The serpentine tube collector has been investigated since the late 1970s [3,6,7]. The analytical study agrees well with single-bend cases and a difference of only 5% was found for cases with any number of bends [3]. They concluded that the analytical model is applicable to large numbers of tubes and the results are acceptable with a small error.

The current study aims to analyze the thermal performance of a sheet-and-tube unglazed PVT collector with serpentine tube configuration. The key objective is to determine  $F_R$  considering the variation in flat plate thicknesses of the plate absorber. Moreover, the optimum thickness for flat plates with the given operating parameters is proposed in this study.

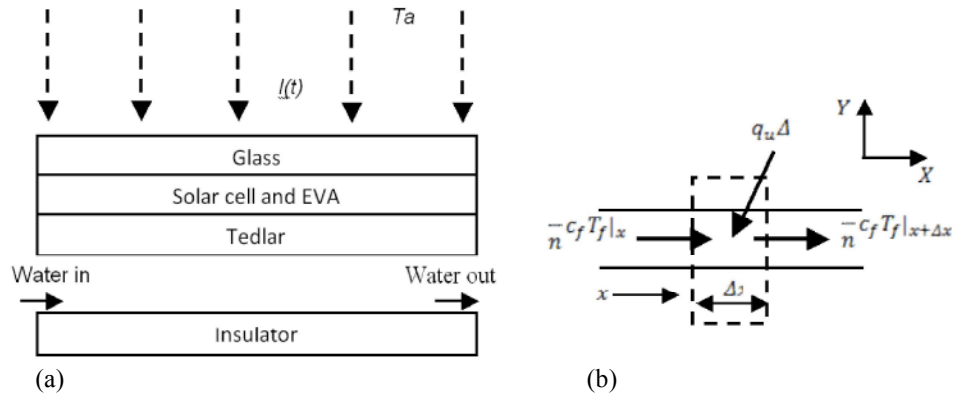


Fig. 1: (a): Cross-section of the unglazed PVT collector, (b) heat flow balance over an element  $\Delta x$  length below the tedlar.

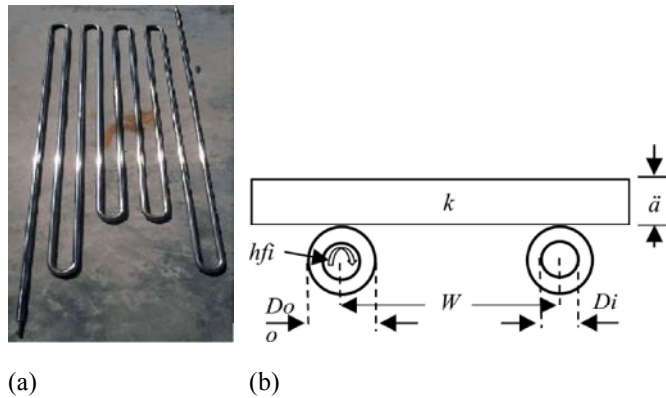


Fig. 3: (a) Serpentine tube arrangement (without plate) and (b) schematic diagram of the serpentine tube collector.

**Thermal Modeling:** An analytical study was conducted to evaluate  $F_R$  of the PVT system. The energy balance of the system was used to estimate  $U_L$  of the unglazed PVT collector. Figures 1(a), 1b (b) and 1(c) show the cross-section of the unglazed PVT collector, the balance of heat flow over an element length  $\Delta x$  underneath the tedlar and the thermal resistance circuit of the PVT system, respectively. The following assumptions were considered to simplify the analysis [8,9]:

- The PVT collector is in a quasi-steady state.
- The transmittance of ethylene vinyl acetate (EVA) is 100%.
- An average temperature is assumed through each layer.
- The flow of water between the tedlar and insulation material (force mode) is uniform.
- Heat conduction is one dimensional.

$U_L$  can be expressed as follows [10]:

$$U_L = U_{tw} + U_b \quad (2)$$

Table 1 shows the PVT parameters used to estimate  $U_L$  based on the thermal energy balance in Equation [10].

$F_R$  of the serpentine tube collector was analyzed after obtaining  $U_L$  for the PVT system. In this study, bond conductance ( $C_b$ ) was neglected to simplify the analysis. Figures 2(a) and 2(b) and Table 2 respectively show the serpentine tube arrangement (without plate), the schematic diagram of the serpentine tube collector and the parameters used for the calculations.

The equations below were used for the analysis [3]. Figure 3 shows the solution of  $F_R$  in terms of three dimensionless parameters known as  $F_1$ ,  $F_2$  and the dimensionless capacitance rate.

The parameters  $F_1$  and  $F_2$  can be obtained as follows respectively [3]:

$$F_1 = \frac{K}{U_L W} \frac{KR(1+\gamma)^2 - 1 - \gamma - KR}{[KR(1+\gamma) - 1]^2 - (KR)^2} \quad (3)$$

$$F_2 = \frac{1}{KR(1+\gamma)^2 - 1 - \gamma - KR} \quad (4)$$

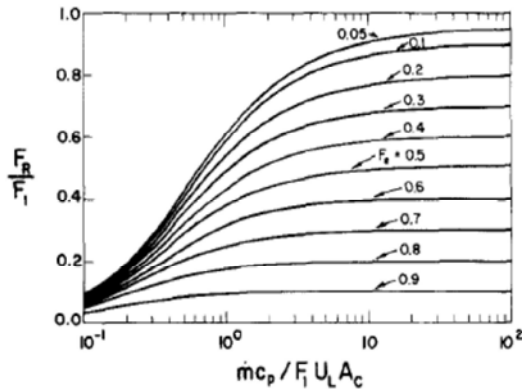


Fig. 4: Heat removal factor ( $F_R$ ) for the serpentine collector plate [3].

Table 1: Parameters for the PVT collector.

Parameter	Value	Unit	Parameter	Value	Unit
$h_i$	5.8	W/m <sup>2</sup> .K	$L_T$	0.0005	m
$h_o$	9.5	W/m <sup>2</sup> .K	$U_b$	0.65	W/m <sup>2</sup> .K
$h_r$	500	W/m <sup>2</sup> .K	$U_L$	8.63	W/m <sup>2</sup> .K
$K_G$	1	W/mK	$U_T$	66	W/m <sup>2</sup> .K
$K_i$	0.035	W/mK	$U_t$	9.24	W/m <sup>2</sup> .K
$K_T$	0.033	W/mK	$U_{Tt}$	8.1028	W/m <sup>2</sup> .K
$L_G$	0.003	m	$V$	1	m/s
$L_i$	0.05	m			

Table 2: Parameters of the serpentine collector.

Parameter	Value	Unit	Parameter	Value	Unit
$L$	1.2	m	$k$	211	W/m. K
$W$	0.06	m	$U_L$	8.63	W/m <sup>2</sup> . K
$N$	9		$m$	0.01	kg/s
$\delta$	0.005, 0.010, 0.015	m	$C_p$	4910	J/kg. K
$Do$	0.015	m	$hf_i$	1000	W/m <sup>2</sup> .K
$Di$	0.009	m			

where

$$k = \frac{(k\delta U_L)^{1/2}}{\sinh[(W-D)(U_L/k\delta)^{1/2}]} \tag{5}$$

$$\gamma = -2\cosh\left[(W-D)\left(\frac{U_L}{k\delta}\right)^{1/2}\right] - \frac{DU_L}{k} \tag{6}$$

$$R = \frac{1}{C_b} + \frac{1}{(\pi D_i h_{f,i})} \tag{7}$$

The dimensionless capacitance rate is given by

$$\frac{\dot{m}C_p}{F_i U_L A_C} \tag{8}$$

## RESULTS

The  $F_R$  results for the various plate thicknesses are presented in Table 3. The highest  $F_R$  of 0.88 was obtained using the 0.015 m-thick flat plate collector, followed by 0.84 and 0.72 for the 0.010 m and 0.005 m-thick flat plate collectors, respectively. The flat plates with the lowest and highest thickness had an approximately 18% difference in  $F_R$ . However,  $F_R$  of the 0.010 m-thick flat plate collector and the highest  $F_R$  had a difference of only less than 5%.

Table 3:  $F_R$  For various flat plate thicknesses,  $\delta$  (m).

$\delta$ (m)	$\frac{\dot{m}C_p}{F_i U_L A_C}$	$F_2$	$F_R / F_1$	$F_R$
0.005	0.500	0.944	0.041	0.72
0.010	0.409	0.954	0.039	0.84
0.015	0.378	0.957	0.038	0.88

## CONCLUSIONS

$F_R$  is a crucial factor in determining the thermal efficiency performance of a serpentine collector. The thickness of a flat plate serpentine collector linearly increases with  $F_R$ . Considering the economic aspect and handling issues, thickness values between 0.010 and 0.015 m area considered within the acceptable range, with only a 4.54% difference in  $F_R$ . A thicker flat plate indicates greater cost and weight, which, in turn, lead to handling issues. Thermal modeling and parametric study are important in determining an economically competitive PVT design.

## ACKNOWLEDGMENT

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## Nomenclature:

- $C_p$  = Fluid specific heat
- $L_T$  = Thickness of tedlar
- $Di$  = Tube inside diameter
- $m$  = Fluid mass flow rate
- $Do$  = Tube outside diameter
- $N$  = Number of segments
- $hf_i$  = Fluid to tube heat transfer coefficient
- $U_b$  = Overall heat transfer coefficient from water to ambient

- $h_i$  = Heat transfer coefficient insulator
- $U_L$  = Overall heat loss coefficient
- $h_o$  = Heat transfer coefficient glass to ambient
- $U_T$  = Conductive heat transfer coefficient from solar cell to water through tedlar
- $h_T$  = Conductive heat transfer through the tedlar
- $U_t$  = Conductive heat transfer coefficient from solar cell to ambient through glass cover
- $k$  = Plate thermal conductivity
- $U_{iT}$  = An overall heat transfer heat transfer coefficient from glass to tedlar through solar cell
- $K_G$  = Conduction of glass
- $U_{iW}$  = An overall heat transfer heat transfer coefficient from glass to water through solar cell and tedlar
- $K_i$  = Conduction of insulator
- $V$  = Wind speed
- $K_T$  = Conduction of tedlar
- $W$  = Distance between tubes
- $L_G$  = Thickness of glass
- $L$  = Length of one serpentine segment

**Greek Letter:**

- $Li$  = Thickness of insulator
- $\delta$  = Plate thickness

**Appendix:** The unknown parameters in Equation (2) are derived as follows:

$$U_{tw} = \frac{h_T U_{tT}}{U_{tT} + h_T}, U_{iT} = \frac{U_T U_t}{U_T + U_t}, U_t = \left[ \frac{L_G}{K_G} + \frac{1}{h_o} \right]^{-1},$$

$$h_T = \left[ \frac{L_T}{K_T} \right]^{-1}, U_b = \left[ \frac{L_i}{K_i} + \frac{1}{h_o} \right]^{-1}, h_o = 5.7 + 3.8V \text{ and}$$

$$U_T = \frac{K_T}{L_T}, A_c = N \times W \times L.$$

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