Hamiltonian Models for Designing Multicasting in All-Ported 3-D Wormhole-Routing Meshes

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Abstract: Multicasting is an information dissemination problem which consists, for a processor of a distributed memory parallel computer, to send a same message to a subset of processors. In this paper, we propose two new multicast algorithms for a mesh network using wormhole routing with the path-based facility. The main feature of the proposed algorithms is its ability to handle multicast operations with a fixed number of message-passing steps irrespective of the network size. Results from extensive comparative analysis reveal that our algorithms exhibit superior performance characteristics over the well-known GIDMFM algorithm.

Key words: Multicasting communication, wormhole routing, hamiltonian model, 3-D mesh, deadlock-free

INTRODUCTION

Optimizing the performance of message-passing multicomputers requires matching inter-processor communication algorithms and application characteristics to a suitable underlying interconnection network. The mesh has been one of the most common networks for existing multicomputers due to its desirable properties, such as scalability, ease of implementation, recursive structure and ability to exploit communication locality found in many parallel applications to reduce message latency. Recent interest in multicomputer systems is therefore concentrated on two or three-dimensional mesh and torus networks. Such technology has been adopted by the Intel Touchstone DELTA [1], MIT J-machine [2], Intel Paragon [3, 4], Caltech MOSAIC [5] and Cray T3D and T3E [6, 7].

The switching method determines the way messages visit intermediate nodes. Wormhole switching has been widely used in practice due firstly to its low buffering requirements, allowing for efficient router implementation. Secondly and more importantly, it makes latency almost independent of the message distance in the absence of blocking [8]. In Wormhole-routed networks, packets are divided into flits. A flit is the smallest unit of information that a channel can accept or refuse. Wormhole routing operates by advancing the head of a packet directly from incoming to outgoing channels [9]. The transmission from the source node to the destination node is done through a sequence of routers. All flits in the same packet are transmitted in order as pipelined fashion. Only the header flit knows where the packet is going and the remaining data flits must follow the header flit. Once the header flit gains access to a channel, the current message owns that channel until the tail flit passes through it and resigns ownership of the channel. If the header encounters a channel already in use, it is blocked until the channel is freed [10].

An important primitive among collective communication operations is multicast communication. Multicast is defined as sending a single message from a source node to a set of destination nodes. In general, the multicasting problem can be modeled by three routing schemes: Tree-based, unicast-based and path-based routing [11]. The tree-based multicasting relies on finding a tree from the underlaid network architecture and the source messages are sent to each destination along the paths on the constructed tree. The unicast-based multicasting sends the messages from source node to destination nodes via intermediate nodes recursively. In path-based facility [12] header consists of a list of destination addresses that must be reached in the specified order. More precisely, a header consists of an ordered sequence of addresses @y1@y2@y3...@yn meaning that the message must go first to y1, next to y2 and so on. When the flits of a message reach an intermediate destination yk, the address @yk is removed from the header and they can be copied to the local memory while they continues in order to reach the next destination specified by the header, namely.
A message is removed from the network when it reaches its last destination. In this way, a message can be delivered to several destinations with the same startup latency as a message sent to a single destination [13].

The performance of multicast communication is measured in terms of its latency in delivering a message to all destinations. Multicast latency consists of three parts, start-up latency network latency and blocking latency [14-20]. The start-up latency is the time required to start a message, which involves operation system overheads. The network latency consists of channel propagation and router delays, i.e., the elapsed time after the head of a message has entered the network at the source until the tail of the message emerges from the network at the destination, while blocking latency accounts for delays due to message contention over network resources, e.g. buffers and channels.

In wormhole routing, contiguous flits in a packet are always contained in the same or adjacent nodes of the network. This can cause difficulties, as possibility of deadlock arises. Deadlock in the interconnection network occurs when a set of messages is blocked forever because each message in the set holds one or more resources needed by another message in this set [21]. No communication can occur over the deadlocked channels until exceptional action is taken to break the deadlock. Many deadlock-free routing algorithms have been developed for wormhole communications networks [9-13, 18, 20, 22-26].

The remainder of this paper is organized as follows. Section 2 presents the system model. Preliminaries are presented in Section 3, including the Hamiltonian models and applying the Hamiltonian model to popular symmetric networks, the 3-D mesh networks.

In Section 4 we introduce the new two multicast algorithms based on the Hamiltonian model while Section 5 compares the performance of the proposed algorithms to the existing GTDMPM algorithm. Finally, Section 6 concludes this study.

**THE SYSTEM MODEL**

This paper, discussion is restricted to the 3-D mesh topology with Bi-directional channels. Figure 1(a) shows (4x4x4) 3-D mesh. The vertices represent the computing nodes and the arcs represent the communication links. The basic node architecture is shown in Fig. 1(b). An m (rows) x n (columns) x r (layers) 3-D mesh comprises mnr nodes interconnected in a grid fashion. The 3-D mesh topology can be modeled as a graph $M (V, E)$ in which each node in $V (M)$ corresponds to a processor and each edge in $E (M)$ corresponds to a communication channel. The mesh graph is formally defined below.

**Definition 1:** An $m \times n \times r$ non-wraparound 3-D mesh graph is a directed graph $M (V, E)$, where the following conditions exist:

$$V(M) = \{(x,y,z) \mid 0 \leq x < m, 0 \leq y < n, 0 \leq z < r \} \quad \text{and}$$

$$E(M) = \{ (x,y,z) \mid (x,y,z) \in V(G), \ 	ext{and} \ |x-x'| + |y-y'| + |z-z'| = 1 \}$$

The mesh topology is asymmetric due to the absence of the wrap-around connections along each dimension. As a result, nodes may not be connected to the same number of neighbors; those at the corners, edges and middle of the network have four and six neighbors respectively. In this system, the node consists of a processing element (PE) and router. The processing element contains a processor and some local memory.

![Fig. 1: (a) The 3D mesh, (b) The node structure in 3D meshes](image-url)
There are local channels used by the processing element to inject/eject messages to/from the network, respectively. Messages generated by the processing element are injected into the network through the injection channel. This study considers the All-Port router model where routers are able to relay multiple messages simultaneously provided that each incoming message requires a unique outgoing channel leading to a neighboring node and that a node can simultaneously send and receive messages along all ejection and injection channels.

PRELIMINARIES

**Hamiltonian schema:** A network partitioning strategy based on Hamiltonian paths is fundamental to the deadlock-free routing schemes. A Hamiltonian path visits every node in a graph exactly once. A Hamiltonian schema can be modeled as a graph \( G = (V, E) \) and \( |V| = N \), we suppose that \( \delta = (v_0, v_1, \ldots, v_{N-1}, v_N) \) is a Hamiltonian path in the graph \( G \). According to the order of the vertex in the Hamiltonian \( \delta \), we can assign each vertex in the graph a label. The label of the vertex \( v \in V \) is denoted as \( \ell(v) \), where \( \ell(v) = i \) is a natural number. That is, the Hamiltonian paths starts at the node labeled 0 and go following the nodes with labels 1, 2, ..., to the node with label N-1 consecutively.

The network partitioning strategy is fundamental to our multicast routing algorithms. After assigning each node a label in the network, we can divide the network into two subnetworks: a high-channel network and a low-channel network. The high-channel network contains all of the directional common channels with the nodes labeled from low to high numbers. The low-channel network contains all of the directional common channels with the nodes labeled from high to low numbers. After partitioning the network into two subnetworks, it is easy to see that every physical communication link lies in one and only one subnetwork, a high-channel network or low-channel network. Each of the two subnetworks has an independent set of physical links in the network. Figure 2(a) shows such a labeling in a 3 x 3 x 3 mesh, in which each node is represented by its integer

![Graphs](image)

Fig. 2: The labeling of a 3x3x3 mesh (a) Physical network, (b) High-channel network, (c) Low-channel network
coordinate \((x, y, z)\). The labeling effectively divides the network into two subnetworks. The high-channel subnetwork contains all of the channels whose direction is from lower-labeled nodes to higher-labeled nodes as shown in Fig. 2(b) and the low-channel network contains all of the channels whose direction is from higher-labeled nodes to lower-labeled nodes as shown in Fig. 2(c).

**Mapping hamiltonian model to 3-D mesh networks:**
A 3-D mesh network contains many Hamiltonian paths. In the following, we give the node labeling function \(\ell(u)\) for a 3-D mesh. The label assignment function \(\ell\) for an \(m \times n \times r\) mesh can be expressed in terms of the \(x-\), \(y-\) and \(z\)-coordinates of nodes as follows:

\[
\ell(x, y, z) = \begin{cases} 
  n^r y + n^z + x & \text{if } z \text{ is even} \\
  n^r y + n^z + (n - x - 1) & \text{if } z \text{ is odd}
\end{cases}
\]  

\hspace{1cm} (2)

The node labeling function will assign each node a unique number. For a 3-D \(m \times n \times r\) the Hamiltonian model starts at the node numbered 0, following the nodes with labels 1, 2, ..., to the node with label \(mnr-1\) consecutively.

**Routing function:** When implementing a multicast routing algorithm, the routing function must be considered. Once a node sends a message to a set of destination nodes, it uses the multicast message preparation algorithm to prepare the destination list in the message header, which will be later sent to the router. The router determines the path for the message according to the routing function. In the following we describe the routing function for the network with Hamiltonian paths model.

The routing function \(R\) for the Hamiltonian model can be viewed as \(R : V \times V \rightarrow V\). It is defined as a function of the node currently holding a message and the destination node of this message. It returns the neighboring node to which the message must be forwarded. More precisely, if \(u\) is the current node and \(v\) is the destination node, then \(R(u, v) = w\), such that \(w\) is a neighboring node of \(u\) and, if \(\ell(u) < \ell(v)\), then we have the following equation:

\[
\ell(w) = \max \{ L(z) | L(z) \leq L(v) \text{ and } z \text{ is a neighboring node of } u \}
\]

or, if \(L(u) > L(v)\), then we have the following equation:

\[
\ell(w) = \min \{ L(z) | L(z) \geq L(v) \text{ and } z \text{ is a neighboring node of } u \}
\]

As proved in [12] this routing function is deadlock-free even using the path-based facility.

**THE PROPOSED ALGORITHMS**

**(TWO-PHASE AND SIX-PHASE)**

This section introduces the Two-Phase (TP for short) and Six-Phase (SP for short) algorithms for All-Port 3-D mesh based on the Hamiltonian model. The proposed algorithms exploit the features of Hamiltonian paths to implement multicast in two and six message-passing steps, thus considerably reducing the effects of both network size and start-up latency. TP is based on splitting the destination set into two disjoint subsets \((D_U, D_L)\), while SP is based on splitting the destination set into six disjoint subsets \((D_{U1}, D_{U2}, D_{U3}, D_{L1}, D_{L2} \text{ and } D_{L3})\) and multicasting the message to these different sets in a pipeline fashion.

**Two-Phase (TP) algorithm:** The Two-Phase algorithm concept for the multicast routing involves restricting the maximal path length that two messages are routed. At the source node, TP algorithm divides the network into two subnetworks, \(N_U\) and \(N_L\), where every node in \(N_U\) has a higher label than that of the source node and every node in \(N_L\) has a lower label than that of the source node. The simple idea of this algorithm is as follows:

**Step 1:** In TP algorithm, a source node divides the destination set \(D\) into two subsets, \(D_U\) and \(D_L\), where \(D_U\) contain the destination nodes in \(N_U\) and \(D_L\) contain the destination nodes in \(N_L\). The messages will be sent from the source node to the nodes in \(D_U\) using the high-channel network \((N_U)\) and to the destination nodes in \(D_L\) using the low-channel network \((N_L)\).

**Step 2:** Sort the destination nodes in \(D_U\), using the \(\ell\) value as the key, in ascending order. Sort the destination nodes in \(D_L\), using the \(\ell\) value as the key, in descending order.

**Step 3:** Construct two messages, one containing \(D_U\) as part of the header and the other containing \(D_L\) as part of the header. The source sends two messages into two disjoint subnetworks \(N_U\) and \(N_L\).

**Step 4:** The TP routing algorithm uses a distributed routing method in which the routing decision is made at each intermediate node. Upon receiving the message, each intermediate node determines whether its address matches that of the first destination node in the message header. If so the address is removed from the message header, the message is copied and sent together with its
header to the above (below) neighboring using the routing function R. In case where the intermediate node is not a destination, it sends the message together with its header to the above (below) neighboring using the routing function R.

**Step 5:** If the sets of the destination nodes are not empty, the algorithm continues according to the previous method.

**Theorem 1:** TP is deadlock-free.

**Proof:** At the source node, TP algorithm divides the network into two disjoint subnetworks. This is obvious since, \( N_U \cap N_L = \emptyset \). Then TP algorithm is deadlock-free at the two subnetworks. Now, we will prove that there are no dependencies within each subnetwork. Since each copy of the message is routed entirely within a single subnetwork and monotonic order (ascending order in \( N_U \) and descending order in \( N_L \)) of requested channels is guaranteed, there cannot exist a cycle within any subnetwork; hence, no cyclic dependency can be created among the channels. So TP is deadlock-free.

**Six-Phase (SP) algorithm:** In a 3-D mesh, most nodes have outgoing degree 6 so up to six paths can be used to deliver a message, depending on the locations of the destinations relative to the source node. The only difference between SP algorithm and TP algorithm concerns message preparation at the source node, in which the destination sets \( D_U \) and \( D_L \) of the TP algorithm are further partitioned. The set \( D_U \) is divided into three subsets, \( D_{U1} \) containing the nodes whose \( x \) coordinates are greater than to that of source, \( D_{U2} \) containing the nodes whose \( x \) coordinates are smaller than to that of source and the \( D_{U3} \) containing the remaining nodes in \( D_U \). The set \( D_L \) is partitioned in a similar manner. The message is sent to the six sets simultaneously through the six output ports of source. Suppose that the coordinate of the source node \( u_0 \) is represented by \((x_0, y_0, z_0)\) and \( D \) represents the destination-set, the message preparation of the SP algorithm is as follow:

**Step 1:** Divide \( D \) into two sets \( D_U \) and \( D_L \) such that \( D_U \) contains all the destination nodes with higher \( \ell \) value than \( \ell(u_0) \) and \( D_L \) the nodes with lower \( \ell \) value than \( \ell(u_0) \).

**Step 2:** Sort the destination nodes in \( D_U \), using the \( \ell \) value as the key, in ascending order. Sort the destination nodes in \( D_L \), using the \( \ell \) value as the key, in descending order.

**Step 3:** Divide \( D_U \) into three sets, \( D_{U1}, D_{U2} \) and \( D_{U3} \) as follows:

\[
D_{U1} = \{ (x,y,z) | (x,y,z) \in D_U, x > x_0, (0 \leq y < m), (0 \leq z < r) \}, \\
D_{U2} = \{ (x,y,z) | (x,y,z) \in D_U, x < x_0, (0 \leq y < m), (0 \leq z < r) \}, \\
D_{U3} = \{ (x,y,z) | (x,y,z) \in D_U, x = x_0, (0 \leq y < m), (0 \leq z < r) \}
\]

![Diagram](image-url)  
*Fig. 3: An example of 4x4x4 mesh*
Fig. 4: The routing patterns of (a) TP algorithm, (b) SP algorithm
Construct three messages, one containing \( D_U \) as part of the header and, second containing \( D_{\Omega} \) as part of the header and the other containing \( D_D \), as part of the header. The source sends three messages to neighboring nodes through \( N_U \) using routing function \( R \).

**Step 5:** Similarly, partition \( D_L \) into \( D_{LL}, D_{L2} \) and \( D_{L3} \) and construct three messages.

**Theorem 2:** The SP is deadlock-free.

The same argument used in the proof of theorem 1 can be used to prove this theorem.

**Comparative study:** As an example, to demonstrate the difference between TP and the SP algorithms, consider the example shown in Fig. 3 for a 4x4x4 mesh topology labeling using a Hamiltonian path. The source node labeled 25 with integer coordinate (1, 1, 1) initiates a multicast to the destination set \( D = \{0, 15, 31, 23, 40, 56, 9, 17, 38, 54, 5, 21, 42, 61, 50, 3, 11, 28, 19, 35, 59\}. 

The TP algorithm splits and sorts, D into two subsets \( D_{\Omega} = \{28, 31, 35, 38, 40, 42, 50, 54, 56, 59, 61\} \) and \( D_L = \{23, 21, 19, 17, 15, 11, 9, 5, 3, 0\} \); the routing pattern is shown with bold lines in Fig. 4(a). The SP algorithm splits destination set first into two subsets, \( D_{\Omega} = \{(3,1,0)), (0,1,0), (3,2,0), (1,2,1), (0,2,2), (2,2,2), (2,3,3), (1,3,2), (0,3,1), (3,3,1), (2,3,0)\} \) with Hamiltonian labels \( \{28, 31, 35, 38, 40, 42, 50, 54, 56, 59, 61\} \) respectively and \( D_L = \{(0,1,2), (2,1,2), (3,1,3), (1,1,3), (0,0,3), (3,0,2), (1,0,2), (2,0,1), (3,0,0), (0,0,0)\} \) with Hamiltonian labels \( \{23, 21, 19, 17, 15, 11, 9, 5, 3, 0\} \) respectively. \( D_L \) is further divided into three subsets \( D_{L1}, D_{L2} \) and \( D_{L3} \), with \( D_{L1} = \{(3,1,0),(3,2,0), (2,2,2),(2,3,3),(3,3,1),(2,3,0)\} \) with Hamiltonian labels \( \{28, 35, 42, 50, 59, 61\} \) respectively, \( D_{L2} = \{(0,1,0), (0,2,2), (0,3,1)\} \) with Hamiltonian labels \( \{31, 40, 56\} \) respectively and \( D_{L3} = \{(1,2,1), (1,3,2)\} \) with Hamiltonian labels \( \{38, 54\} \) respectively. \( D_L \) is also \( D_{L1} = \{(2,1,2), (3,1,3), (3,0,2), (2,0,1), (3,0,0)\} \) with Hamiltonian labels \( \{21, 19, 11, 5, 3\} \) respectively, \( D_{L2} = \{(0,1,2), (0,0,3), (0,0,0)\} \) with Hamiltonian labels \( \{23, 15, 0\} \) respectively and \( D_{L3} = \{(1,1,3), (1,0,2)\} \) with Hamiltonian labels \( \{17, 9\} \) respectively. The routing pattern is shown with bold lines in Fig. 4(b).

Using TP algorithm, Fig. 4(a), number of channels used to deliver the message is 51 (28 in the high-channel network and 23 in the low-channel network). The maximum distance from the source to a destination is 28 hops. Using SP algorithm, Fig. 4(b), number of channels used to deliver the message is 45 channels (24 in the high-channel network and 21 in the low-channel network). The maximum distance from the source to destination is 24 hops. Hence, this example shows that SP algorithm can offer significant advantage over TP algorithm in terms of generated traffic and the maximum distance between the source and destination nodes.

**SIMULATIONS**

To evaluate the performance of the multicast schemes in an interconnection network, there are some parameters that must be considered: the injection rate, the multicast size, the message length and the startup latency. The injection rate is the average interarrival time, the multicast size is the number of destination nodes and the message length is the number of flits in a message. The message startup latency \( \beta \) includes the software overhead for buffers allocating, messages coping, router initializing, etc.

We first give our assumptions to the parameters of system architecture in the simulations. All simulations were performed for a 5x5x5 3-D mesh. We examined the routing performance of our proposed schemes under various injection rate, multicast sizes, startup latencies and message lengths. The source node and the destination nodes for each multicasting were randomly generated. The large message startup latency \( \beta \) is set to be 100 ms and the small message startup latency \( \beta \) is 10 ms. The small message startup latencies were usually used for advanced network interface to improve the efficiency of latency time. For all of the multicasting, the message sizes of 1, 100 and 1000 flits were simulated.

To compare the performance of our proposed multicast routing algorithms, the simulation program used to model multicast communication in 3-D mesh networks is written in VC++ and uses an event-driven simulation package, CSIM [27]. CSIM allows multiple processes to execute in a quasiparallel fashion and provides a very convenient interface for writing modular simulation programs. The simulation program for multicast communication is part of a larger simulator, called MultiSim [28], which is designed to study large-scale multiprocessors. MultiSim consists of several components, all of which run within the CSIM package. This section describes the program and results obtained from it. All simulations were executed until the execution interval execution was smaller than 5% of the mean, using 95% confidence intervals, which are not shown in the figures. To compare the performance of TP and SP to the well known GTDMPM algorithm (The destinations in a multicast message are placed into submulticast messages according to the column, rows and diagonals) [26], 3-D mesh network that contained single channels was used.
Effects of the injection rate and message length: The aim of this first set of experiments is to study the effects of average injection rate on our proposed algorithms. For our first set of simulations, we have fixed the number of destination nodes as 10% of the total number of nodes of the mesh, we have studied three message lengths 1 flit, 100 flits and 1000 flits and two different startup latencies $\beta = 10$ and $\beta = 100$.

Figure 5 and 6 present the performance of average network latency for various network loads on a $5 \times 5 \times 5$ network with small and large message latency respectively. Results are shown for message lengths of 1, 100 and 1000 flits, respectively. It is observed that, the performance of TP and SP algorithms is superior to that of the GTDMPM algorithm. The higher latencies for the GTDMPM algorithm are mainly due to source congestion.

In Fig. 5(a), with small message startup latency the performance of our proposed TP and SP algorithms is superior to that of the GTDMPM algorithm. This difference shows the different strategies to improve the performance of the multicast communication. This implies that the message preparation is the critical part of the multicast routing algorithm. Improvement of the message preparation is more effective to the performance of the multicast communication. TP and SP exhibit good performance at low load. Because message length and message startup latency is very small ($f = 1$ flit, $\beta = 10$), there is no contention in the network due to other multicasts, so two algorithms exhibit good same performance without effect the loads. SP algorithm exhibits slight improvement than TP algorithm.

Figure 5(b) and 5(c) compare three algorithms, again. The message length is 100 and 1000 flits respectively. A gain both TP and SP algorithms obtain better performance over GTDMPM algorithm. This is because the new algorithms implement multicasting with a high degree of parallelism. The performance of the SP algorithm is better than TP algorithm, because,
as shown earlier, paths tend to be shorter, generating less traffic. Hence, the network will not saturate as quickly. For larger injection rate, the network becomes saturated. The SP algorithm saturates lately in any case and GTDMPM algorithm saturates first in any case. The dependencies among message preparation of the GTDMPM become more critical to performance and cause the delay to increase rapidly. The disadvantage of TP algorithm increases with the message lengths as shown in Fig. 5(c). Because the destinations are divided into six sets in SP rather than two in TP, they are reached more efficiently from the source, which is approximately centrally located among the sets, which allows decreasing the lengths of the paths used to reach the destinations. Examining performance results obtained in Fig. 5 do confirm the fact that the performance of GTDMPM is highly dependent on the message length.

In Fig. 6, with large message startup latency, the shapes of the curves are similar to shapes of Fig. 5, they have same analyze as the one for small message startup latency. All the experimental results of section 5.1 show that the best performances are obtained by the SP algorithm. However, the disadvantage of SP algorithm is not appeared until both the load and number of destinations are relatively high as shown in section 5.2.

**Effects of different multicast sizes and message length:** The aim of this second set of experiments is to study the effects of multicast size on our proposed algorithms. In this set of tests, every node generates multicast messages with an average time between messages of 300 µs. We have studied two message lengths 100 flits, 1000 flits and two different startup latencies $\beta = 10$ and $\beta = 100$.

Figure 7 and 8 present the performance of the various multicast schemes on a $5 \times 5 \times 5$ network with small and large message latency, respectively. The results reveal that as the multicast size increases, the performance of the GTDMPM degrades significantly. The GTDMPM do not match the good scalability of the mesh. In contrast, the TP achieves the highest parallelism during multicast operation in all multicast sizes. Furthermore, it manages to maintain a good level of performance irrespective of the multicast size. This is because in the TP, when the multicast size increases,
there is no increase in the number of message-passing steps required to complete the multicast operation. However, the GTDMPM implement the multicast operation in a highly sequential manner, i.e. it require more message-passing steps to implement multicast operations as the multicast size increases.

Figure 7(a) plot the network latency obtained by the three algorithms versus various values of number of destinations, ranging from 20 to 100. In this set of tests, every node generates multicast messages with an average time between messages of 300 μs, the message length is 100 flits and startup latency $\beta = 10$. Notice that, the performance of GTDMPM algorithm worse than that of TP and SP algorithms. This is because the GTDMPM algorithm is a multiple-phase multicasting that needs more startup latency for processing. GTDMPM algorithm saturates faster when the number of destinations is greater than 60. The TP algorithm results in lower latency than the SP algorithm for large destination sets. However, in the SP and GTDMPM algorithms, the source node will send on all of its outgoing channels to reach a large set of destinations. Until this multicast transmission is complete, any flit from another multicast message that routes through that source node will be blocked at that point. The source node becomes a “hot point”. In fact, every node currently sending a multicast message is likely to be a hot point. If the load is very high, these hot points may decrease system throughput and increase message latency. In TP algorithm the source node will send on only two of its outgoing channels, hot points are less likely to occur, the behavior of TP algorithm is stable under high loads with large destination sets. However, the disadvantage of SP algorithm increases with the message lengths under large destination sets as shown in Fig. 7(b). Note that the same conclusion is obtained even when startup latency is set to be 100 as shown in Fig. 8.
CONCLUSION

In this paper, a new two multicast wormhole algorithms in 3-D mesh parallel machines using a path-based facility was presented. These algorithms are shown to be deadlock-free. The proposed algorithms TP and SP have the main advantage of exhibiting a high degree of parallelism and requiring only two and six startups latency message-passing steps respectively irrespective of the destination nodes involved. Furthermore, a performance analysis has revealed that the proposed algorithms have superior latency characteristics over the well known the GTDPM algorithm.

All the experimental results on the average network latency as a function of injection rate show that the best performances are obtained by the SP algorithm; this fact is somewhat independent of the startup time. This was confirmed in Section 5.1. In fact, as shown on section 5.2 which presents experimental results on the average network latency as a function of the number of destinations, “the hot point” is the real cause of the performance degradation for the SP algorithm. The TP algorithm outperforms the SP algorithm for large destination sets independent of the startup time.

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