Predicting for Discharge Characteristics in Langat River, Malaysia Using Neural Network Application Model

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Abstract: Artificial neural networks have been shown to be able to approximate any continuous non-linear functions and have been used to build data base empirical models for non-linear processes. In this study the model are applied to estimate the daily water discharge with two input variables (from two rainfall stations in the same catchments area at Langat River, Malaysia. These model are highly non-linear, therefore two possible ways of analysis is carry out analysis and using the training and testing of sum square error (SSE) we can select the most significant model suit to the case study.

Key words: Artificial Neural networks %non-linear function %river discharge %Langat River

INTRODUCTION

Artificial neural networks have been used in developing non-linear models in industry for such a long time and robustness of the model is one of the main criteria that need to be considered. Robustness of the model can be defined as one of the baseline to judge the performance of the neural network models and it is really related to the learning or training classes [1]. Even though neural networks have a significant capability in predicting a non-linear function, inconsistency of accuracy still seem became a problem where neural networks model seems cannot cope or performed well when it is applied to a new unseen data. Furthermore in this day, that advance process control and supervision of industrial processes require an accurate prediction of the process models and at the same time promoted an interest in robustness of neural networks models. Lack of robustness in neural network models is basically due to the overfitting and poor generalisation of the models (e.g. [2]. Therefore, a lots of researchers was interested and concentrate on how overfitting can be avoided by improved the learning algorithm or by combining the neural networks (e.g. [3-6]. In view of the robustness of neural network a lot of techniques have been developed like regularisation and the early stopping method (e.g. [7-9]. Reference [10] implemented the universal learning rule and second order derivatives to increased the robustness in neural network models.

Case Studies

Study Area: The Langat River is one of the most important river of Malaysia. Many town having very large population like Cheras, Kajang, Sepang and Dengkil are situated along the river bank. In this study the NN model has been applied as a model of short-term water discharge prediction allocation at the selected water quality monitoring station by Department of Irrigation and Drainage in the Langat River, at Selangor, Malaysia. The Langat River Basin occupies the south and south-eastern parts of the state of Selangor Darul Ehsan. It is about 78 km long and ranges from 20 km to 51.5 km wide. It has a total catchment 1,987.8 km². The source of the Langat River is at the Pahang-Selangor border where hilly terrain reaching up to 1,500 m above mean sea level can be found. It finally drains into the Melaka Strait on the mangrove coastline of southwestern Selangor. The major tributaries of the Langat River are Semenyih River, the labu River and the Mantin River. The general flow of the Langat river is north and north-east towards the south and south-west in the eastern half of the basin and westward on the western part.
In general, agriculture and forest are the dominant types of land use in the Langat River Basin. The classification of land use types (in Sq. km.) in the Langat River Basin is shown in Table 1.0. Agriculture is the main land use type (55.13%), followed by forest (19.31%) and wetland (12.73%). Urban and built-up areas only occupy 6.20% of the total land use. Mining (1.61%) is a relatively minor land use type.

Two dams are located in the study area. The Langat Dam in the upstream of the Langat River has an active storage capacity of 30 million m$^3$. Semenyih Dam located in the Semenyih River has an active reservoirs and release water whenever water level of the Langat River is low.

Eight water intakes (water treatment plant) are located in the study area and produce more than 200 MGD (million gallons per day) of treated water. The Langat plant supplies 85 MGD of treated water to areas in Cheras, Pandan and Hulu Langat, while the Cheras Mile 11 plant supplies 6 MGD of treated water to areas in Balakong, part of Cheras and Kajang. The Bukit Tampoi treatment plant supplies 6.9 MGD of treated water to areas of Dengkil. One water treatment plant is located on Semenyih River with Semenyih dam regulation flow to the Semenyih treatment plant. The output capacity of this plant is 120 MGD and supplies treated water to areas in Semenyih, Petaling Jaya South, Bukit Gasing, Shah Alam, Klang and Subang Jaya. Salak Tinggi water treatment plant is located at Salak Tinggi and draws raw water from Labu River. The operator of these plants, Puncak Niaga, constantly monitors the quality of the raw water at intake points.

Neural Network for Time Series and Non-linear Dynamic Relationship: The optimisation method used is the Levenberg-Marquardt algorithm [11, 12]. Regularisation and 'early stopping' method has been used which consist of 100 epoch and the regularisation parameter used is 0.001. Regularisation is achieved by modifying the networks training objective in equation (1) to include a term to penalise unnecessary large network weights as follows:

$$J = \frac{1}{N} \sum_{i=1}^{N} (\hat{y}(i) - y(i))^2 + \rho \| W \|^2$$  \hspace{1cm} (1)

where $N$ is the number of data points, $\hat{I}$ is the networks prediction, $y$ is the target value, $W$ is a vector of networks weights and $D$ is the regularisation parameters. Therefore training will be automatically stop when either one of this criteria is achieved. All weights and biases have been selected randomly in the range of $-0.1$ to $0.1$.

Time Series Prediction: In this case, we carried out 3 different dynamics of the model where the output is the discharge from the catchments area. The time series model can be shown as follows:

a. $\hat{y}(t) = f[y(t-1), y(t-2)]$  \hspace{1cm} (2)
b. $\hat{y}(t) = f[y(t-1), y(t-2), y(t-3)]$  \hspace{1cm} (3)
c. $\hat{y}(t) = f[y(t-1), y(t-2), y(t-3), y(t-4)]$  \hspace{1cm} (4)

By trial and error we carry out analysis which is by varying the hidden neuron from 1 to 10 and plot the training, testing and validation Sum square error (SSE) for all time series model. By using the training and testing SSE we can select the most significant model that suit to the case study.

Non-linear Dynamic Relationship: The dynamic model structure selected for this approach is:

$$\hat{y}(t) = f[y(t-1), y(t-2), u1(t-1), u1(t-2), u2(t-1), u2(t-2)]$$  \hspace{1cm} (5)

where $\hat{I}(t)$ is the models prediction water discharge form the catchments area at time $t$, $y(t-1)$ and $y(t-2)$ are the water discharge at time $(t-1)$ and $(t-2)$ and $u1(t)$ and $u2(t)$ are the raining rates at time $t$ at 2 different station.
Training and Validation Data: To prevent any discrepancy in the unit for the input and output data, all the measurements or the analysis data will be scale down to zero mean and with the same standard deviation. In addition, the comparison on individual SSE for 20 neural networks will be made compare to SSE for combination neural networks and all the simulation and programming work is carried out using Matlab\textsuperscript{TM} 6.5.

Water Catchments Area in Langat River: This area basically a reserve for water supply in area of Sg Rasah in Malaysia. There is a lot of stations that monitor the water flow to the catchments area and in this case we choose two rainfall stations which the number is 2917001 (R\textsubscript{1}) and 3018101 (R\textsubscript{2}) and one water discharge station, the number is 2917401 (Q) that are really related or proportional to the water discharge from the catchments area. Two possible ways of analysis is carried out which is by using time series prediction and 2\textsuperscript{nd} order dynamics of the system. As we know that these models are highly non-linear, therefore the 2\textsuperscript{nd} order system might give some significant improvement in the prediction models. This data consist one year compilation of discharged water (365 daily observation data) from the catchments area and rain falls. We divided the data to training, testing and validation where 100 for training and testing and the rest for validation. The data are normalized using its mean and standard deviation and is shown in Fig. 1.

RESULT AND DISCUSSION

We have trained the network with two input neuron, 1 to 10 hidden neurons and one output neuron. For each neural network performed 10 simulations. The initial weights were randomly chosen in the interval [-1,1]. The results obtained are shown in Table 3 to 6. The first column represents the number of hidden neurons used. The second until fourth column represents the training, testing and validation of SSE.

Table 2 shows the result was obtained for each time series model a, b and c. Model a with five hidden neurons give the best result is a training is 24.938, testing is 60.243 and validation is 114.36. Model b with four hidden neurons, the best result are obtained is a training is 21.73, testing is 63.603 and validation 118.86. While model c with two hidden neuron give the best result is a training is 25.389, testing is 58.443 and validation is 108.05.

Based on this analysis times series model c with hidden neuron of 2 is shows some significant performance to the model. Therefore in time series analysis, model with 2 hidden neuron were used as a basic model for analysis.

It is shown in Table 3 that 2 hidden neuron shows some significant result on the training and testing SSE, therefore 2\textsuperscript{nd} order dynamics system with 2 hidden neuron were used as a basic model for analysis.

Comparison of Models: Fig. 2.0 and 3.0 shows the water discharge (Q) prediction as an example (for the four alternative neural network models investigated) compared to measure validation data set. It would be possible to compare the models predictions to the parameter estimation or training data, however one would expect a good fit in this case as the objective is to minimize the sums of squared errors. The validation set is of key significance, as it indicates the ability of the model generalize. The validation data and the corresponding predictions seem at first sight to be similar to each model with actual data set. It is difficult to assess the
Table 2: SSE of time series model a, b and c

<table>
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<th>b</th>
<th>c</th>
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Table 3: SSE of second order dynamics model

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</table>

performance of the model by looking at such plots and statistical analyses are normally needed.

However from the plotted is given (Fig. 2.0 and 3.0), it shows that the second order model give a good simulation where is the predicted and actual value is close to each other. While for the time series model, it cannot follow the actual value as good as a second order model. The predicted and actual value not too close to each other.

To consider of performance from both model which used in this study, the model comparison is common technique. Statistical test were based on correlation analysis is common in model identification. The correlation analysis as the primary measure of model performance in particular the coefficient of correlation, autocorrelation of the residuals (error between predictions and actual data) and the partial autocorrelation.

For a perfect predictor, the coefficient determination should be +1 or –1. In general the definition of r tells us that 100r^2 is the percentage of the total variation of the predicted values which is explained by, or is due to their relationship with actual values. This is important measure of the relationship between two variables, beyond this scenario, it permits valid comparisons of the strength of several relationships [13, 14, 15].

From the Fig. 4, it can be seen that the scatter plot shows the highly positive correlation for the second order model compare to the time series model c. The coefficient of correlation for the second order model is 0.73 and 0.49 for the time series model.

The autocorrelation function should ideally resemble an impulse. This would indicate that the residuals “white”, i.e. no correlation exists between the residuals and any time shifted replica of the series [16]. There should also be no correlation between the residuals and any linear or
Fig. 2: Water discharge predictions for a time series model (validation data)

Fig. 3: Water discharge predictions for a second order dynamics model (validation data)

Fig. 4: Scatter plot between actual and predicted value of second order model (a) and time series model (b)
non-linear combinations of past inputs and outputs. The autocorrelation and partial autocorrelation of the residuals should exhibit correlation only when the time series are not time shifted (one to the other). If the correlation functions are within a confidence interval of 95% of the conditions mentioned, then it is reasonable to accept the model as a fair representation to simulate of the real data.

The residuals analysis is very useful analysis to help us to identify the performance of the both models. The analysis for the residual are presented in Fig. 5 and 6. It can be seen the autocorrelation and partial autocorrelation function for the second order model is fair enough to achieve the 95% confidence interval (within read line in the figure). While for the time series model c, it fail to
achieve the 95% of the confidence criteria. Where the time series model c shows the two temporal structure for autocorrelation and three temporal structure for partial autocorrelation function out of the 95% confidence criteria.

**CONCLUSION**

Based on SSE produced of each model, two significant models were selected as the best model to simulate water discharge. Time series model c and second order model were selected to comparison for further analysis.

The comparisons of the second order and time series models performance, measured by correlation analysis showed that the second order model had better performance. It can be give a good simulation in the case of water discharge prediction at station 2917401 using two input variables, namely rainfall stations 2917001 and 3018101. The autocorrelation function remained within 95% confidence limits for the most part, as did the partial autocorrelation function.

Based on the results, of the two models investigated, the second order model would be preferred as water discharge modelling at that station.

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