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Hybrid Continuous Wavelet Based Controulet Transform with Generalized Extreme Value Distribution for Dicom Image Compression

[1]C.S. Manikandababu and [2]N.J.R. Muniraj

[1]Senior Grade/ECE, Sri Ramakrishna Engineering College, Coimbatore, India
[2]Tejaa Shakthi Institute of Technology for Women, Coimbatore, India

Abstract: In this paper, Hybrid generalized extreme value distribution based Continuous Wavelet based controulet transform (HGE-CWBCT) is proposed for efficient image compression of DICOM images. The widely used standard for medical image storage and transmission is named as Digital Imaging and Communication in Medicine (DICOM). In every field of medicine including diagnosis, treatment and research, medical images that are obtained as the outputs of the techniques such as the Computerized Tomography (CT), magnetic resonance (MR), digital subtraction angiography (DSA) and Ultrasonography (US) are saved as DICOM format. Network sharing of these larger sized radiology images require large bandwidth. Hence before transferring, compression of such larger image files is necessary for easy and faster communication even with lower bandwidth. Huge amount of data either in multidimensional or multiresolution form is been created as a result of medical information. This makes the following steps like retrieval, efficient storage, management and transmission of these data a complex process. This complexity could be reduced by compressing the medical data without any loss. Many methods have been proposed so far for compression of the large DICOM images, however with some limitations. Thus, specific methods to overcome the limitations like reducing the noise of MSE error signal and improving the PSNR value results in the medical images are to be proposed for the study. The proposed HGE-CWBCT helps for compression of medical images without any data loss and also for improving the PSNR and reducing the MSE of the signal. The directional filter banks are being applied by initializing using the wavelet transform such that the image coding scheme is maintained based on the proposed transform. HGE-CWBCT also uses a new set partitioning in hierarchical trees by employing a sorting method (SPIHT) algorithm that provided an embedded code. In the SPHIT algorithm sorting is performed based on the Dual-Pivot Quicksort (DPQS) algorithm. The performance evaluation of different DICOM and medical images is possible by using parameters like PSNR, MSE and image compression quality measures.

Key words: Generalized Extreme Value Distribution (GEVD) · Wavelet transform (WT) · Controulet transform (CT) · Peak signal to noise ratio (PSNR) · Mean Square error (MSE) · Digital Imaging and Communication in Medicine(DICOM) · Set partitioning in hierarchical trees (SPIHT) · Image compression · Medical Image Processing · Continuous Wavelet transform (CWT)

INTRODUCTION

The growing demand for high speed image transmission, efficient image storage and remote treatment can be met out by introducing an efficient image compression technique. This paper reviews about the different image compression techniques to arrive at a systematic approach for improving the performance of medical image compressing. Among many methods preferred by the medical community, JPEG and wavelet compression are the most popular methods.

Most of the electronic medical records constitute medical images as key components. The storing of these medical records along with its medical images requires enormous space. This makes the network sharing difficult as it consumes more time for transferring such medical

Corresponding Author: C.S. Manikandababu, Senior Grade/ECE, Sri Ramakrishna Engineering College, Coimbatore, India.
E-mail: c.smanikandababu@yahoo.com.

images. Thus on the whole the performance of PACS systems in storing the diagnostic images and other DICOM contents is been improved.

The high speed transfer of image file from one place to another even under lower bandwidth requires compression methods thus reducing the complexity in files communication and sharing [1-2]. Wavelet compression helps for such sharing of medical images and has been proposed knowing its high scope for compressing medical images. The significant part (ROI) is kept separately from the less significant region to be compressed while diagnosing the medical images and is carried out by Discrete Wavelet Transform. The definition of mathematical functions called wavelets over a definite interval carries zero as an average value that helps for data transformation into various frequency components each of which represents its scale of matching resolution [3]. The superposition of any arbitrary function as a basic set of wavelets or functions forms the basis for the wavelet transformation. A single prototype wavelet is called mother wavelet from which the basic set of functions called baby wavelets are derived by means of dilations and translations (shifts) [3]. For two-dimensional capturing of singularities in images, these wavelets are not suitable. Hence, to efficiently capture edges in natural images, several transforms with inherent directionality and multiresolution is to be proposed for image signaling. Examples for such transforms are steerable pyramid [4] and contourlets [5]. One of the new geometrical image transforms is the contourlet transform as the image containing contours and textures [6] is been represented efficiently.

The accurate performance of image compression reduces the complexity of the problem of DICOM image. Therefore, this work focus on proposing a novel method called hybrid generalized extreme value distribution Continuous Wavelet based controulet transform (HGE-CWBCT) method for image compression of DICOM images. Here the wavelet coefficient function x (t) are calculated based on the WPDF that possess a construction as like that the contourlet transform. Also, the non-redundant WBCT is used in conjugation with an SPIHT-like algorithm [7] for constructing an embedded image coder.

A detailed repositioning algorithm for the CWBCT coefficients is also developed owing to parent-child relationship dissimilarities arising between the CWBCT coefficients and wavelet coefficients so that similar spatial orientation trees [7] as used for the wavelet coefficients scanning. The contourlet-based scanning in SPIHT is referred here as CSPIHT. The proposed standard is surely competitive to the original SPIHT coder and is observed from the simulation results. Also the PSNR values suggest that it competes and proves superior to SPIHT coder that too for "non-wavelet-friendly" images having significant amount of textures and oscillatory patterns. The speed of the SPIHT algorithm can be improved by using the criteria of smallest mean-square error and thereby performing Dual-Pivot Quicksort (DPQS) algorithm in the sorting pass of the SPHIT followed by refinement phase by which the most important wavelet coefficients are encoded to show its better compression performance. In this work, a novel wavelet compression method is proposed for DICOM images using HGE-CWBCT and presents novel improved SPHIT coding methods which performs sorting pass based on the Dual-Pivot Quicksort (DPQS) algorithm.

Background Study: By the method of image compression, the amount of data that are kept in a storage media can be increased due to reduction of file size ultimately increasing the data transmission speed. With the help of specialized software, the data of DICOM images are converted into smaller files by compression and the description of it is detailed further in this work. Lossless and lossy are the two main types of data compression and any of these methods are chosen based in the requirement of the system. When the size of any file is compressed without any information losses is termed as lossless compression [8]. Lossy method leads to information loss to some extent with slight observable difference between reconstructed and original images, however providing information more than the compression ratio [9].

Adaptive threshold-based block classification is a newer medical imaging compression technique proposed [10] in which a computational algorithm has been introduced for the classification of blocks based on the adaptive threshold value of the variance. As it is suitable for all types of medical imaging, it is used for the performance evaluation of images derived from CT and ultrasound scanning, X-ray so as to compare the obtained results with JPEG in terms of quality indices. An efficient FPGA implementation of DWT (Discrete Wavelet Transform) and modified SPIHT (set partitioning in hierarchical trees) has been proposed [11] for lossless image compression. The correlation between the image pixels is mainly considered for the DWT (Discrete Wavelet Transform) architecture and is based on the lifting process whereas a modified SPIHT algorithm was helps for encoding the wavelet coefficients. This joint implementation of algorithm promotes both better compression ratio and peak-signal-to-noise ratio (PSNR) for 3D medical images.

The detailed review about the image compression, its necessity and principles, classes and various algorithm is been discussed [12] particularly on the grey scale lena and finger print images. Various compression algorithms based upon wavelet, JPEG/DCT, VQ, fractal was also discussed and their results are compared on the basis of PSNR values and CPU time over encoding and decoding. From these discussions, they arrived at the conclusion of wavelet based compression algorithms highly suitable. An adaptive quantization table must be used by a discrete cosine transform. VQ approach is not suitable for a low bit rate compression however; fractal approach gets suitable by means of its resolution-free decoding property.

3D wavelet transforms [13] for studying a technique called loss to lossless compression in which the approximation process of a 3-D unitary transformation is done by exhibiting a 3-D integer wavelet packet transform structure and by supporting implicit bit shifting of wavelet coefficients. 3D-SPIHT (set partitioning in hierarchical trees) and 3D included sub band coding using optimal truncation process are the 3-D wavelet video coding methods used in their study and found that the results arrived due to loss and lossless compression of volumetric medical images are quite good. The selection of wavelets for compression of medical image is performed by a proposed methodology [14] which dealt on various wavelets transform methods over several metrics like MSE (Mean Square Error), PSNR (Peak Signal Noise Ratio), Structural contents, Normalized Absolute Error etc. for analyzing DICOM CT images. The quality measure is also been taken into consideration for different wavelet type on DICOM CT images. However, wavelets type used in image compression carries no specification remains as a major limitation.

Proposed Methodology: Mostly time lossless compression methods are used in medical applications thus preserving the data integrity facilitating an authentic diagnosis yet its inability to reach high compression ratio is a major disadvantage makes it unsuitable for applications involving telemedicine, fast searching and browsing of medical volumetric data. Lossy compression could be proved to be an alternative for such applications in which volumetric medical images of a studied body part constitutes series of sequences of slices. A single slice among many sequences of slices is been encoded to maintain uniform quality and the decoder receives the compressed bit stream followed by the processing of next sequence of slices. HGE-CWBCT helps for compression of DICOM images which are later encoding through Dual-Pivot Quicksort (DPQS) in the sorting pass by keeping the refinement pass as the same using improved SPIHT algorithm. The complete organization of the proposed medical image compression for method DICOM images is illustrated in Fig. 1.

Hybrid Wavelet Based Controulet Transformation for Image Compression: In contrast to the Laplacian pyramid used in contourlets, two stages of filter bank are present in WBCT in which the first stage enables for decomposition of the DICOM image into subbands, called wavelet transform in WBCT. Calculation of the wavelet coefficient functions for continuous wavelet transformation function having subbands for each DICOM input images are also performed in this stage.

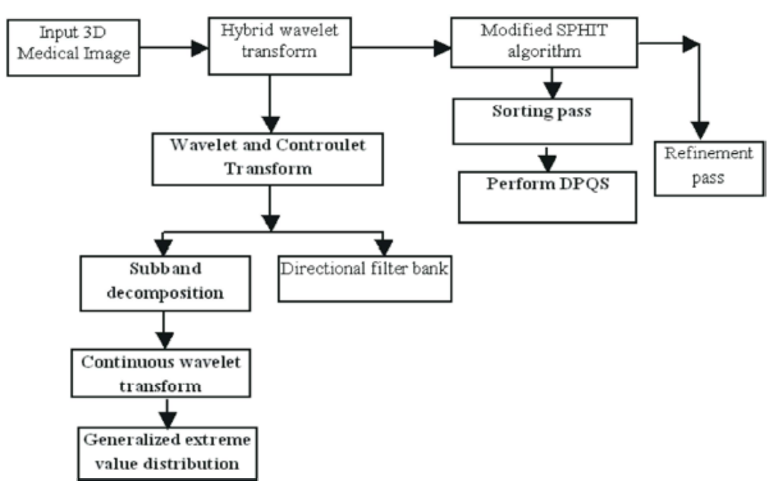

Fig. 1: Structural representation of the proposed work for medical image compression using DICOM images

The angular decomposition is provided by a directional filter bank (DFB), a second stage of WBCT. The separable and non-separable filter banks are been implemented in first and second stage respectively. Using improved SPHIT algorithm single band is encoded after which the compressed bit stream is being sent to the decoder in order to maintain uniform quality for all sequences of subbands, For every DICOM input images, the traditional three highpass bands is obtained corresponding to the LH, HL and HH bands at each level (j), $W(\alpha, b)$ in the continuous wavelet transformation methods. To each band in a given level (j), = $W(\alpha, b)$ DFB with the same number of directions is applied. The number of directions is been decreased while proceeding through the coarser levels ($j < J$) at every other dyadicscale when desired maximum number of directions $N_D = 2$ on the finest level of the wavelet transform $J = f(i)$ is been started. Thus, the anisotropy scaling law; stating *width ≈ lengtl* could be achieved. The value of $x(i)$ is calculated by directly applying the input data of any distribution type and by randomly defining the Square-integrable function $x(i)$ at a scale a > in the wavelet transformation domain. In this study, distribution function based methods are used to calculate the values of the $x(i)$ in the scale parameter by additionally considering the shape parameter (slope) in addition to overcome the difficulties of the CWT transformation methods. This additional consideration of slope results in improvement of the wavelet transformation results than normal Continuous Wavelet transformation (CWT) results by changing the values of the image scale followed by calculation of its decomposition values using:

$$W(a,b) = \frac{1}{\sqrt{a}}\int_{-\infty}^{\infty} x(t)\psi\left(\frac{t-b}{a}\right)dt \tag{1}$$

where a > The considered mother wavelet functions are oscillatory bandpass filters in the time domain. Hence, the basic function is a low frequency function holds a stretched version of the mother wavelet for larger ☻ values and a contracted version called short-duration, high-frequency function for smaller ☻ values. The continuous wavelet function is represented as generalized extreme value distribution with cumulative distribution function,

$$F(x,\mu,\sigma,\xi) = \exp\left\{-1\left[1+\xi\left(\frac{x-\mu}{\sigma}\right)\right]^{-}\right. \tag{2}$$

For $1+\xi\left(\frac{x-\mu}{\sigma}\right) > 0$ where $\mu \in \mathbb{R}$ is the location parameter $\sigma > 0$ the wavelet scale parameter and $\xi \in \mathbb{R}$ the wavelet shape parameter. Thus for $\xi > 0$ the expression just given the cumulative distribution function is valid for $x > \frac{\mu-\sigma}{\xi}$ while for $\xi > 0$ is valid for $x > \frac{\mu-\sigma}{\xi}$, if the value of $\xi > 0$,

$$F(x,\mu,\sigma,\xi) = \exp\left\{-exp\left(\frac{-x-\mu}{\sigma}\right)\right\} \tag{3}$$

without any restriction on wavelet coefficient value x. The density function is, consequently,

$$f(x,\mu,\sigma,\xi) = \frac{1}{\sigma}\left[1+\xi\left(\frac{x-\mu}{\sigma}\right)\right]^{\left(-\frac{1}{\xi}\right)-1}$$

$$\exp\left\{-\left[1+\xi\left(\frac{x-\mu}{\sigma}\right)\right]^{\left(-\frac{1}{\xi}\right)}\right\} \tag{4}$$

Again for $x > \frac{\mu+\sigma}{(\xi)}$ in the case $\xi > 0$ and for $x < \frac{\mu+\sigma}{(-\xi)}$ in the case of $\xi < 0$. The density is zero outside the relevant range. In the case $\xi = 0$ the density is positive on the whole real line and equal to [15],

$$f(x,\mu,\sigma,\xi) = \frac{1}{\sigma}\left[1+\xi\left(\frac{x-\mu}{\sigma}\right)\right]^{1}$$

$$\exp\left\{-\left[1+\xi\left(\frac{x-\mu}{\sigma}\right)\right]^{1}\right\} \tag{5}$$

The transformation becomes irreversible only if it holds the following admissibility condition

$$c_\psi = \int_0^\infty \frac{|\Psi(f)|^2}{|f|}df < \infty \tag{6}$$

The above equation implies that the DC component Ψ((must disappear. Thus, to provide good time resolution, ψ(is a bandpass signal that must sufficiently decayfast. The Parseval relation for the wavelet transform is,

$$\int_{a=0}^{\infty}\int_{b=-\infty}^{\infty} |W(a,b)|^2 \frac{db\ ba}{a^2} = c_\psi \int_{-\infty}^{\infty} |x(t)|^2\ dt \tag{7}$$

The orthonormal wavelet transforms withholds the energy between the different scales that are parameterized by a in the way such that,

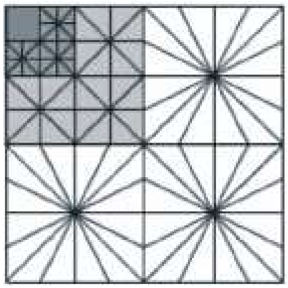
Fig. 2: (a)

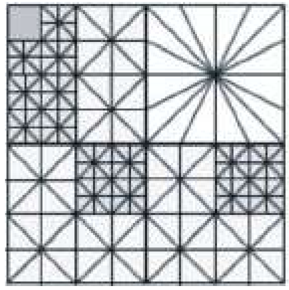
Fig. 2: (b)

$$\int_{a=0}^{\infty} |\psi(t)|^2 \, dt = \int_{-\infty}^{\infty} \frac{1}{|a|} \psi \left| \left(\frac{t-b}{a} \right) \right|^2 dt \quad (8)$$

For the construction of the continuous wavelet transform, the Morlet wavelet becomes a good example of a mother function that is defined by

$$\psi(t) = [\exp(-2i\pi f_0 t) - \exp(-2\pi^2 f_0^2 \sigma^2)] \exp\left(-\frac{t^2}{2\sigma^2}\right) \quad (9)$$

Its Fourier transform is

$$\psi(f) = \sqrt{2\pi\sigma^2}\{\exp[-2\pi^2\sigma^2(f-f_0)^2] - \exp(-2\pi^2\sigma^2 f^2)\exp(-2\pi^2\sigma^2 f_0^2)\} \quad (10)$$

Which satisfies the admissibility condition $\Psi(0)$ =. By choosing this mother function, the continuous wavelet transform upon time discretization $t = n\Delta$ becomes

$$W(a,b) = \frac{\Delta T}{\sigma\sqrt{2\pi a}} \sum_{n=-\infty}^{\infty} s(n) \exp\left[-\frac{(n\Delta T - b)^2}{2a^2\sigma^2}\right] \times \exp\left(-2i\pi f_0 \frac{n\Delta T - b}{a}\right) \quad (11)$$

where Δ is the sampling time in seconds,

The schematic plot of CWBCT is illustrated by the above Fig. 2(a) using 3 wavelet levels and L = directional levels.Logically, partially decomposed DFB's with vertical and horizontal directions on the HL and LH bands has to be used as the DICOM images have vertical directions in the HL image and horizontal directions in the LH. Yet, fully decomposed DFB on each band is completely used as the wavelet filters are imperfect in splitting the frequency space into lowpass and high pass components which means that not all of the directions in the HL image are vertical and in the LH image are horizontal. Wavelet-based Contourlet Packets is almost similar to the Wavelet Packets and is a major advantage of the CWBCT. It is explained by the fact that the quad-tree decomposition of both lowpass and high pass channels in wavelets are allowed by the anisotropy scaling law and on each subband DFB is applied. The schematic illustration of the wavelet-based contourlet packets is given in Fig. 2(b). The proper construction of a quad-tree like angular decomposition which is introduced as Contourlet Packets is possible by ignoring the anisotrophy constraint [16]. Similar to the procedure followed in [5], for an l level DFB, ☻ directional subbands with G^0_k, 0 ≤k≤:< equivalent synthesis filters are given and hence the overall down sampling matrices of G^0_k, 0 ≤k≤:< defined as:

$$S_k^{(l)} = \begin{cases} \begin{bmatrix} 2^{l-1} & 0 \\ 0 & 2 \end{bmatrix} & if\ 0 \le k \le\le 2^{l-1} \\ \begin{bmatrix} 2 & 0 \\ 0 & 2^{l-1} \end{bmatrix} & if\ 2^{l-1} \le k < 2^l \end{cases} \quad (12)$$

Thus, $(g_k^l)[n - S_k^{(l)} m]\}, 0 \le k \le$, $m \in Z$ is a directional basis for $l^2(Z)$ in which g_k^l is the impulse response of the synthesis filter G_k^l. By assuming an orthonormal separable wavelet transforms:

$V_j^2 = V_j \otimes$ and

$$V_{j-1}^2 = V_j^2 \oplus W \quad (13)$$

where W is the detail space and orthogonal component of V in V_j^2. The family $\{\psi_{j,n}^1, \psi_{j,n}^2, \psi_{j,n}^3\}_{n\in}$ is an orthonormal basis of W,l directional levels to detail multi resolution space W, obtain 2 directional of subbands W,

$$W_j^2 = \bigoplus_{k=0}^{2^{l_j}-1} W_{j,k}^{2,(l_j)} \quad (14)$$

Defining

$$\eta_{j,k,n}^{i,(l_j)} = \sum_{n\in Z^2} g_k^{l_j}[m - S_k^{(l_j)} n]\psi_{j,m}^i, i = 1,2..3 \quad (15)$$

The family $\left\{\eta_{j,k,n}^{1,(l_j)}, \eta_{j,k,n}^{2,(l_j)}, \eta_{j,k,n}^{3,(l_j)}\right\}_{n\in}$ is a basis for the subspace $W_{j,k}^{2,(l}$.

Improved Sphit Algorithm for Wavelet Coding: Based on the SPIHT algorithm for wavelet coding of images, the similar concept of spatial orientation tree of wavelet coefficients having a parent-child relationship along wavelet scales, parent-child dependencies in other subband systems can also be found. Depending on the number of directional decompositions in the contourlet subbands [15], two different parent child relationships can be assumed in case of the contourlet transform. If the two

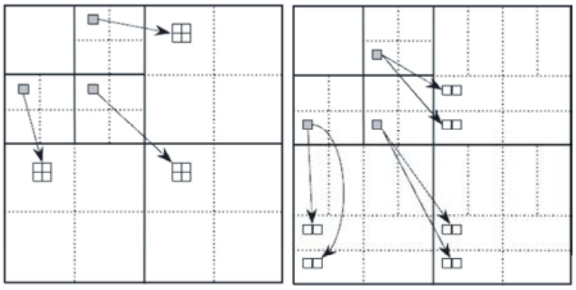

Fig. 3: (a) Fig. 3: (b)

successive scales have the same number of directional decompositions to the parent and children, then both the parent and children would lie in the corresponding directional subbands whereas if the children lie in the scale having twice as many directional subbands as that of the parent, all the four children will be in two adjacent directional subbands. These two directional subbands correspond to the parental location performing directional decomposition of the directional subband. Thus the similarities between WBCT and contourlet transform for each LH, HL and HH subband made us to assume the below illustrated parent-child relationships as shown in Figure 3.

Two possible parent-child relationships in the CWBCT are shown in Fig. 3(a) during which the numbers of directional subbands are the same at the two wavelet scales. However, 4 directions at each wavelet subband as shown in Fig. 3(b) is followed if the number of directional subbands in the finer wavelet scale (say, 8) is twice as given for coarser wavelet scale (say, 4). The set of coordinates representing the coding method is as follows: *0*(*i*) in the tree structures is the set of offspring (direct descendants) of a tree node defined by pixel location (*i, j*)

In DICOM images, *D*(*i*) is the set of descendants of node denoted by pixel location (*i*) in which *L*() is the set defined by $L(i, j) = D(i, j) - 0(i, j)$ The set part itioning trees is defined as below except for the highest and lowest pyramid levels, $O(i,j) = \{(2i,2j),(2i,2j+1),(2i+1,2j),(2i+1,2j+1)\}$

The following are the rules for splitting the set (when identified as significant),

- The initial partition is formed with sets (*i, j* and *D*(*i, j*), for all $(i, j) \in l$
- If *D*(*i* is significant, then it is partitioned into *L*(*i* plus the four single-element sets with $(k, l) \in 0(i, j)$
- If *L*(*i* is significant, then it is partitioned into the four sets D(K with (k,L) ∈ 0(i . In the spatial orientation tree, the significant values of the wavelet coefficients are modeled and stored in three ordered lists namely.
- List of insignificant sets (LIS) containing the set of wavelet coefficients are defined by tree structures and found to have magnitude smaller than a threshold (are insignificant). The coefficient corresponding to the tree or all sub tree roots that are having atleast four elements are being excluded in the sets. The entries in LIS are sets of the type D(i,j) (type A) or type L(i,j) (type E
- List of insignificant pixels (LIP) containing the individual coefficients have magnitude smaller than the threshold.
- List of significant pixels (LSP) containing the pixels are found to have magnitude larger than thethreshold (are significant).

In the sorting pass, the insignificant LIP pixels that are tested in the previous pass and those emerging significant LIP pixels are moved to the LSP. Then, during the sequential assessment of the sets along the LIS order if asset is found to be significant it is removed from the list and partitioned. Based on their significance, the new sets having more than one element are added back to LSP, while adding the one element sets to the end of LIP or LSP. The significance function is defined as follows:

$$S_n(T) = \begin{cases} 1 & \max\{c_{i,j}\} \geq 2^n, (i,j) \in T \\ 0 & otherwise \end{cases} \quad (16)$$

Improved Sphit Algorithm:

Initialization :

Output $n = \log_2(\max_{i,j}\{|c_{i,j}|\})$,set the LSP as an empty set and add the coordinates $(i,j) \in H$ to LIP and only those with descendants also the LIS as type of A entries

Sorting pass:

- For each entry in the LIP do:
- Quick sort algorithm - Dual-Pivot Quicksort (*LIP, I, k*)
- output $S_n(i,j)$
- if $S_n(i,j)$ then move (*i,j*) to the LSP and output the sign of $C_{i,j}$
- for each entry (*i,j*) in this LIS do
- Choose any two LSP as pivot elements P_1 and P_2

- If the selected first P_1 of LSP must be less than P_2 , otherwise they are swapped So, there are the following parts to efficiently performing sorting in the SPHIT methods

- Part I with indices from left+1 to L-1 of the LSP elements which are less than LSP as pivot elements P_1 ,
- Part II with indices from L to K-1 of the LSP elements, which are greater or equal to LSP as pivot elements P_1 and less or equal to LSP as pivot elements P_2
- Part III with indices from G+1 to right-1 of the LSP elements greater than LSP as pivot elements P_2,
- Part IV contains the rest of LSP elements to be examined.

- For each $(k,l) \in O(i,j)$ do output $S_n\ (k,l)$

if S_n = (k,l) = 1 then add (k,l) to the LSP and output the sign of $C_{k,l}$
if S_n = (k,*l*) = 0 then add (k,*l*)to the end of LIP;
if S_n = (k,l) ≠ 1 then move (i,j) to the end of the LIS for type A otherwise, remove entry (*i,j*) from the LIS type B then perform steps 2.2.1 to 2.2.2

- The LSP as pivot elements P_1 is swapped with the last element from part I, the LSP as pivot elements P_2 Is swapped with the first element from part III.
- The steps 1 - 6 are repeated recursively for every part I, part II and part III.

Refinement Pass: For each entry (*i,j*) in the LSP, expect those included in the last sorting pass (i.e., with same n), output the n[th] most significant bit of $|C_{i,j}|$;

Decrement n by 1 and go to Step 2

Dual pivot quick sort algorithm (DPOS) for sorting pass in the SPHIT Algorithm: When the number of the data becomes more, the difficulty in sorting the data in the dataset is solved by using the sorting algorithm to sort the elements in the data or array. It is known as Quick sort that is similar to the wavelet coefficient values in the wavelet transform for SPHIT coding in LIP. It is presented in this work to overcome the problem of sorting of LIP pixels. This tool first divides a large pixels array of high pixel elements into smaller sub-pixels array called as the low pixel elements. Then the sub-pixels arrays are recursively sorted by following the steps involved in the quick sorting:

- From the LIP list, pick anyone of the LIP values randomly and named as pivot element P_1 & |
- Reorder the LIP list based on the randomly selected pivot elements, which is referred as the partition operation in which LIP list starts with lesser pixel value to greater pixel
- Recursively apply the above steps to the sub-LIP Pixels list of elements with lesser values and to the sub LIP of elements separately with greater values.

RESULTS

In this section measure the performance of the proposed Continuous Wavelet Based Controlled transformation (CWBCT) and existing image wavelet compression methods for 3D backbone DICOM images are samples is shown in Fig. 4. The image samples are taken from DICOM sample image sets from http://www.osirix-viewer.com/datasets/. These image samples results are measured using the parameters like Peak signal to noise ratio (PSNR), Mean Square error (MSE), Root Mean Square Error (RMSE).

In Fig. 4 shows the MRI 3D image sample of the backbone, wavelet transformation methods applied samples results is illustrated in Fig. 5, then compressed CWBCT transformation method results is illustrated in Fig.6.

Root-Mean-Square Error (RMSE): Root mean square value is used to measure the results between the predicted values actually observed values. The predicated values is define as $\hat{y}_t$ for times *t* and the actual value is mentioned as the parameter y_t for number of the samples n,

$$RMSE = \sqrt{\frac{\sum_{t=1}^{n}(y_t - \hat{y}_t)^2}{n}} \tag{17}$$

Peak Signal to Noise Ratio (PSNR): Peak signal to noise ratio is used to measure the results of the outcomes and measure the noise value of the image. It is calculated by using following formula,

$$PSNR = 10\log_{10}\left(MAX_I^2/MSE\right) \tag{18}$$

MAX_I is the maximum possible pixel value of the image.

Mean Square Error (MSE): Mean square error (MSE) is defined as the difference amongst an estimator results and the actual of the original images results are computed as,

Table 1: DICOM MRI image results

	MSE (%)		PSNR(dB)		RMSE (%)	
S.NO	WT	CWBCT	WT	CWBCT	WT	CWBCT
1	0.81	0.425	58.4	75.1	0.819	0.42
2	0.83	0.436	49.8	73.25	0.817	0.568
3	0.74	0.415	48.99	76.12	0.825	0.589
4	0.77	0.423	52.4	78.18	0.86	0.54
5	0.79	0.438	59.8	79.2	0.815	0.546

Fig. 4: MRI 3D backbone image

Fig. 5: Wavelet image sample

Fig. 6: Wavelet compressed image sample

$$MSE = \frac{1}{MN}\sum_{i=0}^{M-1}\sum_{j=0}^{N-1}[I(i,j) - K(i,j)]^2 \quad (19)$$

Where I(i denotes the original image and K(i denotes the approximation to the original image which is also called as the decompressed image. M, N is the image dimensions. If the values of the MSE is less it shows the error value of the system is also less, on other hand the PSNR is high. The following Table 1 shows the values of performance comparison results of the WT, CWBCT compression methods with the parameters like MSE, RMSE and PSNR for DICOM Backbone MRI image samples results.

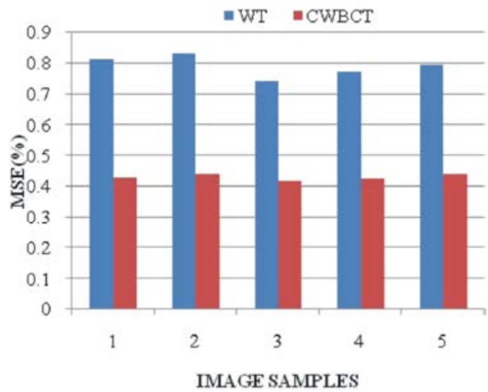

Fig. 7: DICOM Backbone MRI image samples MSE results

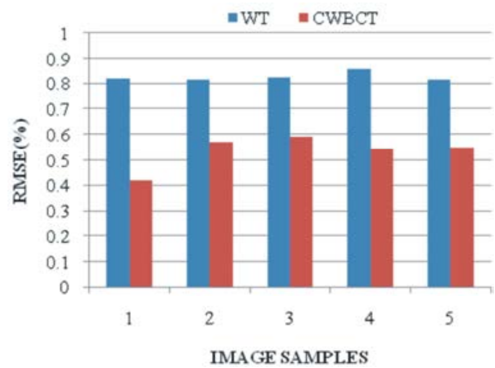

Fig. 8: DICOM Backbone MRI image samples RMSE results

In Fig. 7 illustrates the MSE results of the DICOM Backbone MRI image sample results for five samples between the Wavelet transformation and the proposed Continuous Wavelet Based Controulet Transformation (CWBCT). It shows that the proposed CWBCT have lesser MSE results than the existing wavelet transformation (WT) methods [16].

In Fig. 8 illustrates the RMSE results of the DICOM Backbone MRI image sample results for five image samples between the Wavelet Transformation and the proposed Continuous Wavelet Based Controulet Transformation (CWBCT). It shows that the proposed CWBCT have lesser RMSE results than the existing wavelet transformation (WT) methods.

The above Fig. 9 clearly depicts the comparison of both techniques on the basis of PSNR values. The above results quiet familiarize that the values of continuous wavelet based controulet transformation (CWBCT) is quiet reliable and optimist as compare to Wavelet transform (WT).

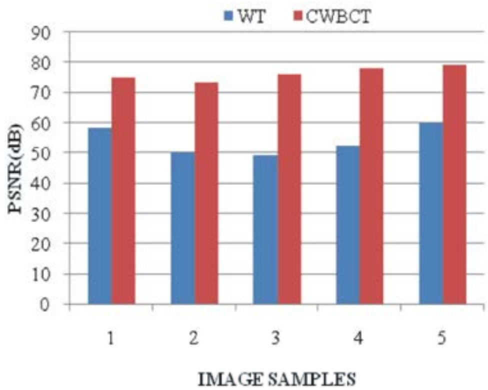

Fig. 9: DICOM MRI image samples PSNR results

CONCLUSION

DICOM is one of the standards followed by now days to maintain the different standards of the medical images in the 3D format. Since due the development of the medical technologies it becomes important to maintain the proper standard for the diagnosis of the diseases of the different patients. In this work, presents a novel wavelet compression of DICOM images using Hybrid generalized extreme value distribution based Continuous Wavelet based controulet transform (HGE-CWBCT) and presents novel improved SPHIT coding methods which performs sorting pass based on the Divot quick sort algorithm (DQSA). The sorting is performed based on the two pivot elements is selected from LIS and sorting is performed with dual pivot element. The performance and accuracy comparison of the DICOM Backbone 3D medical images samples results are measured between the proposed CWBCT compression method and existing WT compression methods using the parameters namely PSNR, MSE and RMSE. The results of the proposed and existing system clearly shown, that the proposed methods have high PSNR, less MSE and less RMSE when compare to existing WT compression methods. In order to further improve the speed of the transformation methods in this work by lattice factorization in wavelet transformation methods. This reduces the time complexity of the system and memory reductions.

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